## Algebra Qualifying Examination, Fall 2019

Instuctions: This is a 3 hour examination. In the problems below, all rings are commutative with identity unless speci ed otherwise. This is a closed book exam, also no notes, searching the web, or otherwise consulting external sources. Good luck!

- 1. Let P be a nite p-group. Show that P is not cyclic if and only if P has a quotient isomorphic to Z=pZ Z=pZ.
- 2. Let R be a commutative ring with unity.

(a) Let S be a non-empty saturated multiplicative set in R, i.e. if a; b2 R, then ab2 S if and only if a; b2 S. Show that R S (the complement of S in R) is a union of prime ideals.

(b) Supposerythat R Buppolomain such that evenythengrenceppeime(C) 912a0 Us (CT33att)] Torther 33 accords diagonal matrix.

(b) If F is an algebraically closed eld and A 2 GL<sub>N</sub>(F) is of nite order, is