ALGEBRA QUALIFYING EXAM FALL 2018

Exercise 1. Suppose *p* is a prime. Show that the Galois group of $x^5 = 1 \ 2 \ F_p[x]$ depends only on *p* (mod 5), and compute it for each congruence class of *p* (mod 5).

Exercise 2. Let *R* be a Dedekind domain with eld of fractions *K* Show that for any two proper fractional ideals I; J there are ; 2 K with I; J R integral and I + J = R.

Exercise 3. Suppose that *R* is a Noetherian ring and \mathfrak{p} *R* is a prime ideal such that $R_{\mathfrak{p}}$ is an integral domain. Show that there is an $f \ge Rn\mathfrak{p}$ such that R_f is an integral domain where R_f