ALGEBRA QUALIFYING EXAM SPRING 2018

Exercise 1. Suppose p is a prime. Show that the Galois group of x^5 1.2 $F_p[x]$ depends only on p (mod 5), and compute it for each congruence class of (mod 5).

Exercise 2. Let R be a Dedekind domain with eld of fractions K Show that for any two proper fractional ideals I;J there are f: G with f: G with f: G integral and f: G and f: G with f: G integral and f: G and f: G with f: G integral and f: G integral and f: G in the same f: G integral and f: G in the same f: G integral and f: G in the same f: G integral and f: G integral and f: G in the same f: G integral and f: G in the same f: G integral and f: G in the same f: G integral and f: G integral and f: G in the same f: G integral and f: G in the same f: G integral and f: G in the same f: G integral and f: G in the same f: G in the same f: G integral and f: G in the same f: G integral and f: G in the same f: G i

Exercise 3. Suppose that R is a Noetherian ring and p R is a prime ideal such that R_p is an integral domain. Show that there is an f 2 R n p such that R_f is an integral domain where $R_f = S^{-1}R$ with S = f 1